

## REFERENCES

- [1] A. J. Seeds and J. R. Forrest, "Initial observations of optical injection locking of an X-band IMPATT oscillator," *Electron Lett.*, vol. 14, pp. 829-830, Dec. 1978.
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### Further Comments on "Integration Method of Measuring $Q$ of the Microwave Resonators"

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In reply to our comments [1] concerning his paper,<sup>1</sup> I. Kneppo showed an exact integration of the expression

$$P(\omega) = P_0 [1 + Q_L^2 (\omega/\omega_0 - \omega_0/\omega)^2]^{-1} \quad (1)$$

between the limits  $\omega_1$  and  $\omega_2$  by the substitution of variables,  $x = \omega/\omega_0 - \omega_0/\omega$ , and a simplifying choice of limits symmetrical in  $x$

$$I = \int_{\omega_1}^{\omega_2} P(\omega) d\omega = P_0 \omega_0 Q_L^{-1} \tan^{-1}(Q_L \omega_2 \omega_0^{-1}). \quad (2)$$

Limits symmetrical about  $x = 0$  amount to the condition

$$\omega_1 \omega_2 = \omega_0^2 \quad (3)$$

and when this relation holds, (2) is exact as may be verified by substituting (3) into the general expression for  $I$ , regardless of integration limits

$$I = \frac{P_0 \omega_0}{2Q_L} \left\{ \tan^{-1} \left[ \omega_0 Q_L \frac{\omega_2(\omega_0^2 - \omega_1^2) - \omega_1(\omega_0^2 - \omega_2^2)}{(\omega_0^2 - \omega_1^2)(\omega_0^2 - \omega_2^2)Q_L^2 + \omega_1 \omega_2 \omega_0^2} \right] \right. \\ \left. - 2 \frac{1}{\sqrt{4Q^2 - 1}} \ln \left[ \frac{(\omega_0^2 + \omega_2^2)Q_L + \omega_2 \omega_0 \sqrt{4Q_L^2 - 1}}{(\omega_0^2 + \omega_1^2)Q_L - \omega_1 \omega_0 \sqrt{4Q_L^2 - 1}} \right] \right. \\ \left. - \frac{(\omega_0^2 + \omega_1^2)Q_L - \omega_1 \omega_0 \sqrt{4Q_L^2 - 1}}{(\omega_0^2 + \omega_2^2)Q_L + \omega_2 \omega_0 \sqrt{4Q_L^2 - 1}} \right\} \quad (4)$$

and using the identity

$$2 \tan^{-1} a = \tan^{-1} \frac{2a}{1 - a^2}. \quad (5)$$

We had assumed [1] integration limits symmetrical in  $\omega_0$

$$\begin{aligned} \omega_1 &= \omega_0 - \omega_s/2 \\ \omega_2 &= \omega_0 + \omega_s/2 \end{aligned} \quad (6)$$

rather than  $x$ , but this does not account for the difference between our results and Kneppo's for typical microwave cavities.

Unfortunately, (7) in [1] omitted the square on  $Q_L$  in the denominator of the  $\tan^{-1}$  term, this equation being otherwise identical to (4) of this note. Thus, our approximations for the case  $Q_L \gg 1$ ,  $\omega_0 \gg \omega_s$  were in error. When (6) is substituted in (4), given these conditions, Kneppo's (2) results.

It follows that (8) and (9) in our comments [1] are in error and that (10) should read

$$I = 2\pi P_0 \Delta f \tan^{-1} k. \quad (7)$$

In any case, the method of integrating (1) between general limits is of much interest, and (4) does allow asymmetrical limits for experimental integration. For example, integrating between the 3-dB and the resonant frequencies (setting  $\omega_1$  or  $\omega_2$  equal to  $\omega_0$ ) gives

$$\frac{I}{P_0} = \frac{\pi^2 \Delta f}{4} \quad (8)$$

where  $\Delta f$  is the 3-dB bandwidth. This expression should allow a check on the symmetry of the resonance curve and, hence, show how good a description of the cavity resonance (1) actually is.

## REFERENCES

- [1] P. L. Overfelt and D. J. White, "Comments on 'Integration method of measuring  $Q$  of the microwave resonators'," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-31, pp. 502-504, June 1983.

### Comments on "New Narrow-Band Dual-Mode Bandstop Waveguide Filters"

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I have read the above paper<sup>1</sup> with interest, but find some possible discrepancies between the data presented in Fig. 4 and the data presented in Fig. 6. It seems to me that the data in Fig. 4 is probably accurate, reflecting as it does the rejection obtainable through a single pair of ports coupling to a dominant mode propagating waveguide. No matter how the multiple pole filter is synthesized in the concept discussed by the authors, the shunt coupled bandpass filter is coupled only by a pair of couplings to the main line. Thus, the limitation on the depth of the obtainable rejection is determined by two factors: 1) orthogonality of the two coupling irises, and 2) return loss of the two coupling irises.

The data of Fig. 6 implies an input return loss for the bandpass filter and a value for the coupling iris isolation of over 50 dB, values which do not seem very likely. The data of Fig. 4 shows

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<sup>1</sup>J.-R. Qian and W.-C. Zhuang, *IEEE Trans. Microwave Theory Tech.*, vol. MTT-31, pp. 1045-1050, Dec. 1983.

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<sup>1</sup>I. Kneppo, *IEEE Trans. Microwave Theory Tech.*, vol. MTT-31, Feb. 1978.